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A sensorless control for a variable speed wind turbine operating at partial load

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ABSTRACT

This paper presents a sensorless control for a variable speed wind turbine (WT) operating at partial load in order to eliminate the direct measurement of the wind speed. In this proposal, the estimated aerodynamic torque is used to determine the optimal reference of the speed control for maximum energy conversion. The maximization of the efficiency on energy conversion and the minimization of detrimental dynamical loads are control trade-offs considered in the design of an optimal discrete-time feedback LQG/LTR controller for the Wind Energy Conversion System (WECS), which is based on the optimization of a quadratic cost function. The performance of the proposed control when the WT is submitted to a gust or step variation on wind speed is evaluated from computational simulations. It is also presented some proposals for sensorless control of the electrical generator.

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1. Introduction

Due to significant cost reductions, improved efficiency and the increased useful life provided by the technological development of wind energy conversion systems (WECS), wind power is considered one of the most attractive solutions to energy problems. The basic configuration of a WECS is shown in Fig. 1. It is composed by a wind turbine (WT) coupled to an electrical generator, directly or through gear-box. In spite of its simplicity, the WECS represents an interesting problem in viewpoint of the control theory, since it is a nonlinear system, subjected to cyclical disturbances caused by operational phenomena, and highly dependent of a stochastic variable characterized by sudden variations. Thus, the quality of a WECS controller is determined by its capacity to deal with model uncertainties, exogenous stochastic signals, and periodic disturbances.

Although classical methods are traditionally utilized in WECS control, these solutions are not completely adequate since the resulting controllers do not provide sufficient damping to system and the necessary robustness to uncertainties, such as parameter variations, nonlinear behavior, etc [1–5]. In this context, the linear quadratic gaussian controller with loop transfer recovery (LQG/LTR) consists in an interesting alternative for WECS, since it combines the necessary characteristics to assure the stability margin, disturbance attenuation and a reasonable robustness to model uncertainties [6,7]. Furthermore, the control trade-offs for a WECS can be easily translated into a quadratic cost function [3,8], which is inherent to design of an optimal linear feedback LQG/LTR controller.

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The information related to wind speed is essential for the control of a WECS. However, the use of anemometers to measure the wind speed can represent a serious obstacle to implement a robust control structure for a WECS [9,10]:

- The possible contamination of the reference signal by the wind fluctuation, which can be solved filtering the measurement signal;
- The wind speed can not be measured exactly in the WT rotor, which difficulties the exact evaluation of the available power for energy conversion;
- The installation of the anemometer can reduce the reliability of the measure of wind speed due to aerodynamic interference, shadowing effects, turbulences, etc.

Another fundamental information for WECS control is the position or the rotation of mechanical shaft, which can be measured using tachometers, encoders and resolvers. However, the use of these transducers can also introduce others problems:

- These transducers are often one of the most expensive and fragile components in a WECS, principally for small and medium power systems;
- The space limitations and difficult access to the mechanical shaft can implicate in restrictions to use of a speed sensor;
- The additional wires for electrical connections of a speed sensor can increase the vulnerability of the system to electro-magnetic interferences (EMI);
- Problems related to assembling and maintenance.



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Fig. 1. Basic WECS configuration.

Thus, the direct measurement of the wind speed, position and rotation of the mechanical shaft can represent a great obstacle to the implementation of a more efficient, robust and cheap WECS, since the related sensors can be extremely expensive and introduce several uncertainties in the system. In this context, the elimination of the direct measurements of the mechanical variables in the control system consists in a very attractive perspective in the technical and economical viewpoints for WECS design, principally for small and medium systems.

This paper presents a sensorless control for a variable speed WT operating at partial load, aiming the elimination of the direct measurement of the wind speed. In this proposal, the estimated aerodynamic torque is used to determine the optimal reference of the speed control for maximum energy conversion. The maximization of the efficiency on energy conversion and the minimization of detrimental dynamical loads are control trade-offs considered in the design of an optimal discrete-time feedback LQG/LTR controller for the Wind Energy Conversion System (WECS), which is based on the optimization of a quadratic cost function. The performance of the proposed control when the WT is submitted to a gust or step variation on wind speed is evaluated from computational simulations. It is also presented some proposals for sensorless control of the electrical generator.

2. Nonlinear WECS model

The WECS dynamics are presented in Fig. 2. For the computational simulation of the system, it is necessary a complex and consistent nonlinear WT model that consider several operational phenomena, such as losses, wind shear, ripple torque, and turbulence. Assuming

a single dimensional random process, a nonlinear dynamic model for WT system can be divided in four distinct subsystems [11]: wind, aerodynamics, driven train and electrical generator. In the approach adopted in this paper, the structural dynamics are neglected and considered as model uncertainties.

2.1. Wind

An adequate model of the wind is necessary to predict the dynamics of a WECS. Although the wind is a multidimensional stochastic process, which depends on the time and spatial coordinates, a two dimensional model is generally enough to describe adequately this phenomenon [11]. The wind speed V_H at the reference height H can be given by [12,13]:

$$V_H = \overline{V} + \Delta V + V_G + V_R \tag{1}$$

where \overline{V} is the effective average of the wind speed over the WT rotor and ΔV is the wind fluctuation given by:

$$\Delta V = 2 \sum_{i=1}^{N} [S_{\nu}(\omega_i) \Delta \omega]^{\frac{1}{2}} \cos(\omega_i t + \Phi_i)$$
⁽²⁾

where $\omega_i = (i - (1/2))\Delta\omega$, Φ_i is an independent random variable with uniform density in the interval of $0-2\pi$ and $S_v(\omega_i)$ is the power spectral density, given by [11]:

$$S_{\nu}(\omega_{i}) = \frac{2K_{N}F^{2}|\omega_{i}|}{\pi^{2}\left[1 + \left(\frac{F\omega_{i}}{\mu\pi}\right)^{2}\right]^{\frac{4}{3}}}$$
(3)



Fig. 2. WECS dynamics.

where K_N is the superficial drag coefficient, F is the turbulence scale, and μ is the average of the wind speed in the reference height. For good results, it is suggested N = 50 and $\Delta \omega$ between 0.5 and 2.0 rad/s [14]. Since the wind speed depends of the height due to "wind shear", an approach to compute the wind speed at a specific height h is given by [11,15,16]:

$$V_h = V_H \left(\frac{h}{H}\right)^a \tag{4}$$

where *a* is a coefficient that depends of the local topography. Considering the blade geometry, the wind speed V_i in the representative point 3/4 of the cord of the *i*-th blade can be expressed as:

$$V_i = V_H \left\{ 1 + \frac{3}{4} \frac{R}{H} \sin(\theta_{Bi}) \right\}^a$$
(5)

where θ_{B_i} is the spacial angle of the *i*-th blade. An essential component to study the dynamical behavior of a WECS is the discrete longitudinal gust V_G . Considering that a wind gust begins at instant T_G and finishes after ΔT_G , this component can be estimated as [14,17,18]:

$$V_{G} = \frac{3\overline{V}_{H}}{2\ln\left(\frac{H}{h_{o}}\right)} \left\{ 1 - \exp\left(-\frac{\overline{V}_{h}\Delta T_{G}}{1.48h}\right) \right\}^{\frac{1}{2}} \left[1 - \cos\left(2\pi\frac{t - T_{G}}{\Delta T_{G}}\right) \right]$$
(6)

for $T_G < t < T_G + \Delta T_G$, where the parameter h_o is the roughness height. Another important component of the wind speed is the ramp V_R described as [14]:

$$V_R = V_{RMAX} \left(\frac{t - T_R}{\Delta T_R} \right) \tag{7}$$

for $T_R < t < T_R + \Delta T_R$, where V_{RMAX} is the peek of the ramp, T_R is the initial instant when the ramp begins and ΔT_R is ramp duration. For small ΔT_R , the ramp component can be used as an approach of the wind step.

2.2. WT aerodynamics

An accurate model for the aerodynamic behavior of a WT is often very difficult to obtain due to the uncertainties in its description. The aerodynamic behavior of the WT is nonlinear, dependent of wind speed and may change over time due to contamination of blade surfaces. In general, the best approach to evaluate the aerodynamic torque Q_a uses dimensionless coefficients C_p and C_q , which respectively express the WT ability to convert kinetic energy of moving air into mechanical power or torque [8,19]. Besides dependency of constructive aspects of the WT blades, both coefficients C_p and C_q are nonlinear functions of the yaw angle θ and a parameter known as tip-speed ratio λ , which is defined as:

$$\lambda = \frac{R\omega_t}{V} \tag{8}$$

where R = turbine radius, $\omega_t =$ WT speed and V = wind speed. Admitting that WT is always aligned with wind direction, i.e. $\theta = 0^\circ$, the aerodynamic torque Q_a in a blade of WT is given by [8,11,15]:

$$Q_a = \frac{1}{2}\rho AR \frac{C_p(\lambda)}{\lambda} V^2 = \frac{1}{2}\rho AR C_q(\lambda) V^2$$
(9)

where $\rho = \text{air}$ density and A = rotor area. Typical $C_p \times \lambda$ and $C_q \times \lambda$ characteristics of a WT are shown in the Fig. 3.



Fig. 3. Aerodynamic characteristics of a WT.

2.3. Driven train

The driven train can be modeled as a set of masses coupled through flexible connections as shown in Fig. 4 [8,20]. Although the gear-box has nonlinear characteristics [21], this component can be supposed ideal. Using the classical rotational dynamics to describe the coupling system of a WT with n blades:

• *i*-th blade:

$$J_i\dot{\omega}_i + D_i\omega_i = Q_{ai} - D_{ih}(\omega_i - \omega_h) - Q_{mih}$$
(10)

• hub:

$$J_h \dot{\omega}_h + D_h \omega_h = \sum_{i=1}^n [D_{ih}(\omega_i - \omega_h) + Q_{mih}] - D_{hg}(\omega_h - \omega_g) - Q_{mhg}$$
(11)

• electrical generator:

$$J_g \dot{\omega}_g + D_g \omega_g = D_{hg} (\omega_h - \omega_g) + Q_{mhg} - Q_g$$
(12)

• shaft torques:

$$\dot{Q}_{mih} = K_{ih}(\omega_i - \omega_h) \tag{13}$$

$$\dot{\mathbf{Q}}_{mhg} = K_{hg}(\omega_h - \omega_g) \tag{14}$$

where $\omega_i = i$ -th blade speed, $\omega_h = hub$ speed, $\omega_g = generator$ speed, $J_i = i$ -th blade inertia, $J_h = hub$ inertia, $J_g = generator$ inertia (including the gear-box inertia), $D_i = i$ -th blade damping, $D_h = hub$ damping, $D_g = generator$ damping, $D_{ih} = i$ -th blade-hub connection damping, $D_{hg} = shaft$ damping, $K_{ih} = i$ -th blade-hub connection stiffness, $K_{hg} = shaft$ stiffness, $Q_{ai} = i$ -th aerodynamic torque, $Q_{mih} = i$ -th blade torque, $Q_{mhg} = shaft$ torque and $Q_g = generator$ torque.

2.4. Electrical generator

The electrical generator constitutes the link between the rotational mechanical energy and the available electrical power to



Fig. 4. Driven train model.

costumers. Since the dynamics of electrical systems are extremely fast when compared to mechanical coupling, a quasi-static model can be assumed for electrical generator. Considering the use of a current controlled static converter as the interface between the generator and the electrical load, the generator torque Q_g is perfectly adjustable in all operating bandwidth and virtually independent from WECS dynamics [8], consisting in the only control input of a stall regulated WT.

3. Nominal linearized model for control design

For robust control design, it is necessary to derive a simplified and linearized mathematical model of the WT. Observing the typical characteristic $C_q \times \lambda$ of a WT shown in Fig. 3, two distinct operating regions can be identified [8,22,23]:

- The stall region (A), characterized by a positive slope of the curve $C_q \times \lambda$, where the operation is unstable and a sudden and significant drop in the aerodynamic torque occurs due to phenomenon known as aerodynamic "stall";
- The normal operation region (B), characterized by a negative slope of the curve $C_q \times \lambda$, which corresponds to normal operation of WT.

The linearization of the aerodynamic torque Q_a can be performed in the specific point of maximum C_p , which is always situated in the normal operating region. In this operating point, $\lambda = \lambda_{opt}$ and the derivatives $\partial C_p / \partial \omega_t$ and $\partial C_p / \partial V$ are null. The linearized aerodynamic torque Q_a around maximum C_p is given by:

$$\dot{\mathbf{Q}}_a = \alpha \dot{\mathbf{V}} + \gamma \dot{\omega}_t \tag{15}$$

where α is the scaling factor of the torque disturbance due to wind variations \dot{V} , and γ denotes the acceleration feedback coefficient from drive-train. In steady state, \dot{V} is the wind fluctuation, which can be assumed as an uncorrelated in the time zero-mean Gaussian stochastic signal [11]. Considering \overline{V} as the nominal wind speed, the coefficients α and γ can be computed from WT data as:

$$\alpha = \frac{\partial Q_a}{\partial V}\Big|_{\lambda_{opt}} = \frac{3}{2}\rho A R \frac{C_{pmax}}{\lambda_{opt}} \overline{V}$$
(16)

$$\gamma = \frac{\partial Q_a}{\partial \omega_t}\Big|_{\lambda_{opt}} = -\frac{1}{2}\rho A R^2 \frac{C_{pmax}}{\lambda_{opt}^2} \overline{V}$$
(17)

Although a real mechanical drive train has rigid disks connected by a flexible shaft, where the inertias and compliances are distributed along its length, an approximated lumped 2-mass model presented in Fig. 5 is enough to obtain a good indication of the dynamical loads for control design [8,15]. Admitting an ideal gearbox and reducing all quantities to primary side, the mechanical coupling can be described using classical rotational dynamics [12]:

$$J_t \dot{\omega}_t + D_t \omega_t = Q_a - Q_{mhg} - D_{hg} (\omega_t - \omega_g)$$
(18)

$$J_g \dot{\omega}_g + D_g \omega_g = D_{hg} (\omega_t - \omega_g) + Q_{mhg} - Q_g$$
(19)

$$\hat{Q}_{mhg} = K_{hg} (\omega_t - \omega_g) \tag{20}$$



Fig. 5. Approximated lumped drive train model.

where $\omega_t = WT$ speed, $J_t = \text{total WT}$ inertia and $D_t = \text{total WT}$ damping.

The structural dynamics and the nonlinearities can be admitted as uncertainties. Thus, the nominal linearized state model of a stall regulated WT for control design is given by:

$$\dot{\boldsymbol{x}}(t) = \boldsymbol{A}\boldsymbol{x}(t) + \boldsymbol{b}\boldsymbol{Q}_{g}(t) + \boldsymbol{\psi}$$
(21)

 $y(t) = \mathbf{c}\mathbf{x}(t) + \boldsymbol{\xi} \tag{22}$

where $\mathbf{x}(t) = [Q_a \quad \omega_t \quad \omega_g \quad Q_m]'$ and the disturbance input on the system due to wind fluctuation \dot{V} is given by $\boldsymbol{\psi} = [\alpha \dot{V} 0 \ 0 \ 0]'$. Due to practical constraint relatives to assembling, cost and maintenance of sensors, the generator rotation ω_g , contaminated by the measurement noise ξ , is considered the only measured output *y*. The matrices **A**, **b** and **c** are given by:

$$\mathbf{A} = \begin{bmatrix} \frac{\gamma}{J_t} & -\frac{\gamma(D_t + D_{hg})}{J_t} & \frac{\gamma D_{hg}}{J_t} & -\frac{\gamma}{J_t} \\ \frac{1}{J_t} & -\frac{D_t + D_{hg}}{J_t} & \frac{D_{hg}}{J_t} & -\frac{1}{J_t} \\ 0 & \frac{D_{hg}}{J_g} & -\frac{D_{hg} + D_g}{J_g} & \frac{1}{J_g} \\ 0 & K_{hg} & -K_{hg} & 0 \end{bmatrix}$$
$$\mathbf{b} = \begin{bmatrix} 0 & 0 & -\frac{1}{J_g} & 0 \end{bmatrix}'$$

4. Some control requirements

 $\mathbf{c} = \begin{bmatrix} 0 & 0 & 1 & 0 \end{bmatrix}$

For medium- to large-scale systems, the controller design can be difficult from a numerical point of view, since the involved matrix operations tend to be ill-conditioned [4]. Although both speed and power can be selected as the controlled variable in a WECS, the speed control is considered dynamically better than the power control [24]. In this case, the WECS must be operated at fixed λ_{opt} to maximize the energy conversion. This strategy can compromise the control performance due to the direct dependence of the rotation reference with the wind speed, which is always varying and can not be measured exactly at the WT rotor.

Another problem in a WECS is the propagation of vibrations and ripple torque on the system with undesirable consequences on energy quality and lifetime of several system components. Sudden variations in the wind can excite torsional modes, which can cause unacceptable mechanical efforts on the drive train. Although the aerodynamic stall provides the speed limitation for high wind speed, it is necessary to avoid operation in the stall region in order to obtain a better WECS performance [15]. Thus, the control design has to establish a trade-off between the dynamical loads in the system and the increase of the energy conversion. Given the multiple aspects of WECS global efficiency (reliability, availability, remote operation, quality of captured power, etc.), the WECS optimal control implies the necessity of adopting mixed-criteria optimization indices [25].

The poles of the closed-loop system must be assigned as far away as possible from the frequencies related to the greatest energy density of dynamical loads. Furthermore, it is necessary to obtain sufficient gain and phase margins to assure a safe stability margin, since the WECS uncertainties can not be quantified due to the complexity of interactions between WT and wind field. According to Leith e Leithead [12], practical experience suggests that a gain margin of 10 dB and a phase margin of roughly 60° are sufficient to assure the control design robustness for any WECS.

5. LQG/LTR methodology

The discrete-time LQG/LTR methodology consists in the formal establishment of a quadratic performance index to synthesize a linear feedback regulator K_c . Considering a discrete-time state model (Φ , Γ , Ψ , Π), the Linear Quadratic Regulator (LQR) provides a control signal that minimizes the following cost function [7,26]:

$$J = \sum_{k=0}^{\infty} [\mathbf{z}'(k)\mathbf{Q}\mathbf{z}(k) + \mathbf{u}'(k)\mathbf{R}\mathbf{u}(k)]$$
(23)

where $\mathbf{z}(k)$ corresponds to target outputs. The targets and the control input are weighted respectively by matrices \mathbf{Q} and \mathbf{R} , and the resulting discrete-time regulator $\mathbf{K}_{\mathbf{c}}$ is given by:

$$\mathbf{K}_{\mathbf{c}} = \left[\mathbf{R} + \mathbf{\Gamma}' \mathbf{P} \mathbf{\Gamma}\right]^{-1} \mathbf{\Gamma}' \mathbf{P} \boldsymbol{\Phi}$$
(24)

where **P** is the definite positive solution of the following discretetime Riccati equation:

$$\mathbf{P} = \mathbf{Q} + \boldsymbol{\Phi}' \mathbf{P} \boldsymbol{\Phi} - \boldsymbol{\Phi}' \mathbf{P} \boldsymbol{\Gamma} [\mathbf{R} + \boldsymbol{\Gamma}' \mathbf{P} \boldsymbol{\Gamma}]^{-1} \boldsymbol{\Gamma}' \mathbf{P} \boldsymbol{\Phi}$$
(25)

Since the LQR provides a infinite gain margin and at least 60° for phase margin [7], which is enough to assure the WECS stability, the regulator design can be concentrated in to obtain an effective performance for dynamical response. An adequate choice of targets **z** and weighting matrices **Q** and **R** allows to establish a quadratic performance index of the LQR similar to the cost function for WECS control described by Leithead et al. [3], which involves the trade-offs between efficiency on energy conversion and the dynamical loads.

The optimization of the energy conversion is an important control requirement for variable speed WECS, and depends on the accuracy of speed control. Thus, the speed error $\varepsilon = \omega_{ref} - \omega_g$ can be used as an indication of efficiency conversion, and its inclusion in the LQR performance index implies a model expansion. In this way, the state model given by eqs. (21) and (22) is discretized for (**A**_d, **B**_d, **C**_d, **D**_d) and augmented to insert the speed error ε as a new state variable. The following discrete-time state model is then obtained:

$$\overline{\mathbf{x}}(k+1) = \overline{\mathbf{\Phi}}\overline{\mathbf{x}}(k) + \overline{\mathbf{\Gamma}}\mathbf{Q}_{g}(k)$$
(26)

$$\overline{\mathbf{y}}(k) = \overline{\mathbf{\Psi}}\overline{\mathbf{x}}(k) \tag{27}$$

where $\varepsilon(k)$ is the discrete summation of the speed error, the new state vector is $\overline{\mathbf{x}}(k) = [\varepsilon(k) \quad \mathbf{x}'(k)]'$ and $\overline{\mathbf{y}}(k)$ corresponds to new output. For discrete-time LQG/LTR controller design, the inclusion of this integral action assures the elimination of steady state errors. Hence the discrete-time matrices $\overline{\Phi}$, $\overline{\Gamma}$ and $\overline{\Psi}$ are given by:

$$\overline{\boldsymbol{\Phi}} = \begin{bmatrix} 1 & -\mathbf{C}_{\mathbf{d}}\mathbf{A}_{\mathbf{d}} \\ \mathbf{0}_{4\times 1} & \mathbf{A}_{\mathbf{d}} \end{bmatrix}$$

$$\overline{\Gamma} = \begin{bmatrix} -\mathbf{C}_{\mathbf{d}}\mathbf{B}_{\mathbf{d}} & \mathbf{B}_{\mathbf{d}} \end{bmatrix}'$$
$$\overline{\Psi} = \begin{bmatrix} 1 & \mathbf{0}_{1\times 4} \end{bmatrix}$$

Another important control requirement is to minimization of the detrimental dynamical loads, which are basically determined by mechanical torques and speeds. One of these dynamical loads are the torsional modes, which depend on the difference $\Delta \omega = \omega_t - \omega_g$. To reduce the stress on the shaft, the variations on the shaft torque Q_s must be minimized over all bandwidth. The control design has also to minimize the effects of wind fluctuation and ripple torque over the energy delivered to electrical load, which is represented in the WECS model by the generator torque Q_g . Thus, the targets can be chosen as $\mathbf{z}(k) = \mathbf{M}\mathbf{x}(k)$, where the matrix \mathbf{M} is:

$$\mathbf{M} = egin{bmatrix} 1 & 0 & 0 & 0 & 0 \ 0 & 0 & 1 & -1 & 0 \ 0 & 0 & 1 & 0 & 0 \ 0 & 0 & 0 & 1 & 0 \ 0 & 0 & D_{hg} & -D_{hg} & 1 \end{bmatrix}$$

Since the weighting matrices are selected as $\mathbf{Q} = diag(w_1, w_2, w_3, w_4, w_5)$ and $\mathbf{R} = w_6$, the performance index of the LQR regulator is converted into:

$$J = \sum_{0}^{\infty} \left[w_{1}(\varepsilon)^{2} + w_{2}(\Delta \omega)^{2} + w_{3}(\omega_{t})^{2} + w_{4}(\omega_{g})^{2} + w_{5}(Q_{s})^{2} + w_{6}(Q_{g})^{2} \right]$$
(28)

The relative importance of each target on the index to be minimized by the LQR action is determined by its respective weight w_i , which establishes the intensity of the control action on a specified target. The use of weights dependent on frequency (weighting functions) increases the flexibility on targets manipulation, allowing to penalize selectively a determined bandwidth. However, weighting functions increases the controller complexity due to addition of extra dynamics to the original model. The selection of the weights w_i depends strongly on the system configuration and the inevitable design trade-offs.

The complement of the LQG/LTR controller design consists in the determination of the discrete-time Kalman filter for optimal estimation of the state variables, which will be used as the exact measurements by LQR. This filter estimates the state vector $\hat{\mathbf{x}}(k/k)$ from actual measurement vector $\mathbf{y}(k)$, taking the following form [27]:

$$\widehat{\mathbf{x}}(k+1/k) = \overline{\boldsymbol{\Phi}}\widehat{\mathbf{x}}(k/k-1) + \overline{\boldsymbol{\Gamma}}\mathbf{u}(k) - \overline{\boldsymbol{\Phi}}\mathbf{K}_{\mathbf{f}}\left(\overline{\boldsymbol{\Psi}}\widehat{\mathbf{x}}(k/k-1) - \mathbf{y}(k)\right)$$
(29)

$$\widehat{\mathbf{x}}(k/k) = \widehat{\mathbf{x}}(k/k-1) - \mathbf{K}_{\mathbf{f}}\left(\overline{\Psi}\widehat{\mathbf{x}}(k/k-1) - \mathbf{y}(k)\right)$$
(30)

Assuming the state and measurement noise covariance matrices W and V, K_f is given by:

$$\mathbf{K}_{\mathbf{f}} = \mathbf{P}\overline{\boldsymbol{\Psi}}' \left(\overline{\boldsymbol{\Psi}} \mathbf{P} \overline{\boldsymbol{\Psi}}' + \mathbf{V} \right)^{-1}$$
(31)

where **P** is the positive semidefinite solution of the Riccati equation:

$$\mathbf{P} = \overline{\boldsymbol{\Phi}} \mathbf{P} \overline{\boldsymbol{\Phi}}' - \overline{\boldsymbol{\Phi}} \mathbf{P} \overline{\boldsymbol{\Psi}}' \left(\overline{\boldsymbol{\Psi}} \mathbf{P} \overline{\boldsymbol{\Psi}}' + \boldsymbol{V} \right)^{-1} \overline{\boldsymbol{\Psi}} \mathbf{P} \overline{\boldsymbol{\Phi}}' + \mathbf{W}$$
(32)

The complete WECS controller is synthesized by connection of the Kalman filter to LQR, as shown in Fig. 6. However, the inclusion of the Kalman filter can imply in the degradation of robustness and performance properties obtained in the LQR design. It is possible to recover these properties through the LTR procedure (Loop Transfer Recovery), which consists in an adequate choice of the covariance matrices **V** and **W** in the Kalman filter design [6,7,27]. This procedure also allows the asymptotic closed-loop poles placement, avoiding undesirable frequencies [26].

6. Sensorless control

For maximum energy conversion, the speed reference ω_{ref} must be directly proportional to wind speed to assure the WT operation at λ_{opt} . This strategy can reduce the control robustness due to problems related to wind speed measurement. However, the optimal speed reference ω_{ref} for the control system can be indirectly obtained, avoiding the necessity to measure the wind speed. From eq. (9), the following relationship is obtained considering the WECS operating at λ_{opt} :

$$\omega_{ref} = K_{qa} \sqrt{Q_a} \tag{33}$$

where K_{qa} is a constant value given by:

$$K_{qa} = \frac{\lambda_{opt}}{R} \sqrt{\frac{2\lambda_{opt}}{\rho ARC_{pmax}}}$$
(34)

Since the aerodynamic torque Q_a measurement is not directly available, it is estimated from the preceding data using a Kalman predictor, as shown the Fig. 7. Considering the nominal WECS model described in section 2, the dynamics of the Kalman predictor is given by eq. (29), where the gain K_f is computed using the eqs. (31) and (32) [27]. The covariance matrices W and V must be selected for a slowest response if compared to feedback controller, aiming a good filtering of the speed reference and the decoupling between predictor and controller dynamics.

There are several proposed strategies for the elimination of a sensor to measure the shaft speed of an electrical motor that can used in the case of the generator. The most of these



Fig. 6. LQG/LTR control structure for WECS.



Fig. 7. Sensorless controller for WT: Optimal speed reference determination.

strategies is based in the estimative of back emf (in the case of the generator, emf), a phenomenon that depends of the rotor speed which can be estimated from the machine voltage and current measurements [28-31]: from a dynamical model, an adaptive observer is designed to estimate the states and the rotor speed. The drawback of this strategy is its inherent dependence with the machine parameters, which becomes the speed estimation sensible to parameter uncertainties [32]. The second strategy is the injection of a high frequency voltage wave in the machine terminals to induce a current signal, which depends of the rotor position [33]. However, this strategy requires constructive modifications in the machine aiming to avoid torque pulsation [32]. The third strategy consists in the monitoring of the harmonic components produced by rotor slots, which filtering provides signal equivalent to an incremental encoder which resolution is $p(N_r+1)$ pulses per revolution, where p = number of pole pairs of the machine and $N_r =$ number of slots per pole pairs [34].

7. Simulation results

The performance of the proposed sensorless control structure is verified from computational simulations considering a Horizontal Axis WT shown in the Fig. 8 with two blades of 45.72 m

Vind 91,44m 15,72m 91,44m 91,44m 15,24m 91,44m 15,24m

Fig. 8. Horizontal Axis WT used in computational simulations.

each, which normalized data in relation to its rated values (2.5 MW and 17 RPM) are presented in Table 1. The WECS is simulated using the nonlinear model presented in section 2. The control structure is designed using the nominal linearized model described in section 3, considering a sample interval of $T_s = 5$ ms and a nominal wind speed of $\overline{V} = 6.7m/s$. The weights for LQR are chosen as $w_1 = 500$, $w_2 = 500$, $w_3 = 100$, $w_4 = 100$, $w_5 = 100$ and $w_6 = 1$. The covariance matrices for the Kalman filter design are selected as $\mathbf{V} = \varepsilon \psi' \psi$ and $\mathbf{W} = 10^{-3}$. Using the LTR procedure, the parameter ε is adjusted to 10^5 to obtain a good properties recovery. The Kalman predictor is designed selecting the covariance matrices as $\mathbf{V}_{\mathbf{pred}} = T_s^2 \psi \psi'$ and $\mathbf{W}_{\mathbf{pred}} = \alpha^2$. The frequency response of the open-loop control system can be verified by Bode diagrams shown in Fig. 9, where the infinite gain and phase margins indicate a stable close-loop control system.

The first simulated event is the wind gust shown in Fig. 10. Its is observed in Fig. 11 that the LQG/LTR controller provides an accurate adjustment for generator speed ω_g . Thus, the WECS operates practically closed at constant λ as shown in Fig. 12. Since system losses are not considered, the speed reference obtained by the Kalman predictor is slightly below the ideal reference. None torsional mode is excited by this wind gust. The control system imposes an adequate attenuation for wind flutuaction and ripple torque, avoiding the propagation of dynamical loads to other parts of the WECS, as can be observed in Figs. 11 and 13.

Since a WT can be submitted to sudden wind variations, the second simulated event to verify the closed-loop dynamics is a wind step. Considering the operation at a mean wind speed of 6.7 m/s, it is suddenly varied to 8.9 m/s after 20 s as shown the Fig. 14. In face of the increase on wind speed, the controller increases the generator speed (Fig. 15) to maintain λ constant (Fig. 16), assuring the WECS operation almost in maximum efficiency on energy conversion. None torsional mode is excited by this wind step. It is observed in Figs. 15 and 17 that the control system continues imposing an adequate attenuation for wind flutuaction and ripple torque for a wind speed of 8.9 m/s. In this context, the fatigue on drive-train components is reduced, improving the quality of generated energy.

Table 1 WT normalized data.

$J_t = 37.413$	$D_t = 2.024 \times 10^{-2}$
$K_{hg} = 28.4$	$D_{hg} = 1.831$
$J_g = 2.091$	$D_g = 3.01 imes 10^{-2}$

Bode Diagram Gm = Inf dB (at Inf rad/sec) , Pm = Inf



Fig. 9. Bode diagrams for open-loop WECS control system.



Fig. 10. Wind gust.

Fig. 11. Normalized speeds for the wind gust.



Fig. 14. Wind step.

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8. Conclusions

This paper presents a sensorless control for a variable speed WT operating at partial load, that feeds an electrical load through static power converters. The speed reference is obtained from a Kalman predictor, which estimates the aerodynamic torque and avoids the direct wind speed measurement. This procedure is very attractive. since the complexity and the uncertainty of wind measurement can compromise the robustness of the control system. The LQG/LTR methodology was applied to design an optimal discrete-time feedback controller for a WECS. Since this methodology automatically assures the stability margin for the close-loop system, the control system is designed to obtain an effective performance for dynamical response through an adequate choice of targets and weighting matrices, establishing a formal cost function to be minimized by control action. The objective is to increase the efficiency on energy conversion, reducing the detrimental dynamic loads caused by wind fluctuation and ripple torque. Considering a consistent nonlinear dynamical model for WT system as the real plant, a wind gust and a step variation on wind speed are simulated to verify the closed-loop system performance. The simulation results have shown that the proposed sensorless control structure provides a WECS operation near the maximum efficiency point, reducing the influence of vibrations and ripple torque and, consequently, the stress over the mechanical drive system.

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